Reteaching 11-4

Arithmetic Series

OBJECTIVE: Finding the sum of a given number of terms of a series

MATERIALS: None

Example

Evaluate the series $\sum_{n=2}^{4} (5-2n)$.

$$\sum_{n=2}^{4} \boxed{(5-2n)}$$

$$n = 2$$

$$(n = 3)$$

$$n = 4$$

- Circle the upper and lower limits. Box the explicit formula.
- ✓ In circles, write all possible values of n, beginning with the lower limit and ending with the upper limit.

$$(n=2)$$

$$(n=3)$$

$$n = 4$$

$$5 - 2(2)$$

$$5 - 2(3)$$

$$5 - 2(4)$$

Under each circle, draw a box; copy the explicit formula, substituting the value in the circle above the box for the value of n.

$$\sum_{n=2}^{4} (5-2n) = \boxed{5-2(2)} + \boxed{5-2(3)} + \boxed{5-2(4)}$$

$$= 1 + (-1) + (-3)$$

- The value of the series is the sum of the values in the boxes.
- **Evaluate each expression.**
- Find the sum of the terms.

The sum of the series is -3.

Exercises

Evaluate each series.

1.
$$\sum_{n=1}^{3} (n-4)$$

2.
$$\sum_{n=1}^{4} \frac{1}{3n}$$

3.
$$\sum_{n=3}^{8} (3n-1)$$

4.
$$\sum_{n=3}^{8} \frac{2n}{3}$$

5.
$$\sum_{n=3}^{9} (4-2n)$$

6.
$$\sum_{n=1}^{5} 8n$$

7.
$$\sum_{n=2}^{7} 4n$$

8.
$$\sum_{n=1}^{7} (3-2n)$$

9.
$$\sum_{n=2}^{5} (5n+1)$$

10. An outdoor amphitheater has 45 rows of seats. The first row has 89 seats. The last row has 177 seats. Each row has 2 more seats than the previous row. Write an explicit formula representing the number of seats in the *n*th row. Then find the sum of the 45 rows of seats.